

1. Average-of-primes sequence:  $s_1 = 2$ ,  $s_n = \frac{1}{2}(p_{2n-2} + p_{2n-1})$  for all  $n \geq 2$  where  $p_i \equiv i$ th prime

2, 4, 9, 15, 21, 30, 39, 45, 56, 64, 72, 81, 93, 102, 108, 120, 134,

144, 154, 165, 176, 186, 195, 205, 225, 231, 240, 254, 266, 274, 282, 300,

312, 324, 342, 351, 363, 376, 386, 399, 414, 426, 436, 446, 459, 465, 483,

495, 506, 522, 544, 560, 570, 582, 596, 604, 615, 625, 642, 650, 660, 675,

687, 705, 723, 736, 747, 759, 771, 792, 810, 822, 828, 846, 858, 870, 882,

897, 915, 933, 944, 960, 974, 987, 1003, 1016, 1026, 1036, 1050,

1062, 1078, 1092, 1100, 1113, 1126, 1152, 1167, 1184, 1197, 1215, ...

2. Average-of- $k$ -primes sequence:  $s_n = \left[ \frac{p_{(n-1)k+1} + p_{(n-1)k+2} + \dots + p_{nk}}{k} \right]$  where  $p_j$  is the  $j$ th prime and  $[x] \doteq$  integer nearest to  $x$ . If  $x = \frac{y}{2}$  for an odd integer  $y$  then set  $[x] = x - \frac{1}{2}$ .

•  $k = 2$ :

2, 6, 12, 18, 26, 34, 42, 50, 60, 69, 76, 86, 99, 105, 111, 129, 138,

150, 160, 170, 180, 192, 198, 217, 228, 236, 246, 260, 270, 279, 288, 309,

315, 334, 348, 356, 370, 381, 393, 405, 420, 432, 441, 453, 462, 473, 489,

501, 515, 532, 552, 566, 574, 590, 600, 610, 618, 636, 645, 656, 667, 680,

696, 714, 730, 741, 754, 765, 780, 803, 816, 825, 834, 855, 861, 879, 885,

909, 924, 939, 950, 969, 980, 994, 1011, 1020, 1032, 1044, 1056,

1066, 1089, 1095, 1106, 1120, 1140, 1158, 1176, 1190, 1207, 1220, ...

•  $k = 3$ :

3, 10, 20, 32, 44, 58, 70, 84, 100, 110, 132, 146, 162, 178, 194, 211,

230, 244, 263, 276, 294, 314, 338, 354, 373, 390, 410, 428, 444, 460, 478,

498, 518, 548, 568, 586, 602, 616, 638, 653, 670, 692, 718, 738, 756, 776,

806, 824, 840, 860, 880, 902, 928, 947, 972, 990, 1014, 1028, 1046, 1064, 1090,

1103, 1123, 1156, 1180, 1202, 1223, 1239, 1272, 1288, 1300, 1316, 1352, 1384,  
 1420, 1434, 1450, 1470, 1486, 1501, 1532, 1554, 1572, 1594, 1610, 1622, 1652,  
 1676, 1702, 1726, 1747, 1773, 1792, 1822, 1858, 1874, 1890, 1917, 1944, 1980, ...

- $k = 4$ :

4, 15, 30, 46, 64, 81, 102, 120, 144, 165, 186, 207, 232, 253, 274, 298,  
 324, 352, 375, 399, 426, 447, 467, 495, 523, 559, 582, 605, 627, 650, 673,  
 705, 735, 759, 791, 820, 844, 870, 897, 931, 959, 987, 1015, 1038, 1061,  
 1092, 1113, 1149, 1183, 1213, 1236, 1274, 1294, 1312, 1357, 1403, 1432, 1452,  
 1480, 1498, 1536, 1562, 1590, 1612, 1635, 1673, 1706, 1736, 1768, 1797, 1840,  
 1872, 1894, 1931, 1972, 1998, 2021, 2056, 2085, 2113, 2138, 2174, 2219, 2250, 2277, 2302,  
 2340, 2364, 2386, 2412, 2446, 2480, 2533, 2559, 2602, 2639, 2667, 2688, 2707, 2730, ...

3. Prime-pairs-and-sums sequence (Two rules: One – Any prime  $p$  such that  $p - 2$  or  $p + 2$  is also prime is included in the sequence; Two – For primes  $p$  and  $q = p + 2$ ,  $p + q$  is also included, unless both  $p + q - 1$  and  $p + q + 1$  are both prime. The latter rule is enforced so as to ensure the absence of consecutive triples  $a, a + 1, a + 2$  in the sequence):

3, 5, 7, 8, 11, 13, 17, 19, 24, 29, 31, 36, 41, 43, 59, 61, 71, 73, 84, 101,  
 103, 107, 109, 120, 137, 139, 144, 149, 151, 179, 181, 191, 193, 197, 199, 204, 216...

4. 2-adic expansion sequence for primes (1 if the 2-adic expansion of prime  $p$  has an odd number of terms, and 0 otherwise):

1, 0, 0, 1, 1, 1, 0, 1, 0, 0, 1, 1, 1, 0, 1, 0, 1, 1, 1, 0, 1, 0, 0, 1,  
 0, 1, 1, 1, 0, 1, 1, 1, 0, 0, 1, 1, 0, 1, 1, 1, 1, 0, 1, 1, 1, 1, 1, ...

5. 3-adic expansion sequence for primes (1 if the 3-adic expansion of prime  $p$  has an odd number of terms, and 0 otherwise):

1, 1, 0, 0, 0, 1, 1, 0, 1, 0, 1, 1, 0, 0, 1, 0, 1, 1, 0, 0, 1, 0, 0, 1, 0,  
 1, 0, 0, 1, 0, 0, 1, 1, 0, 1, 1, 1, 0, 1, 1, 0, 0, 0, 1, 0, 0, 1, ...