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Vexillary Involutions are Enumerated by Motzkin Numbers

O. Guibert¹, E. Pergola², and R. Pinzani²

¹LaBRI (UMR 5800), Université Bordeaux 1, 351 cours de la Libération, 33405 Talence cédex, France

guibert@labri.u-bordeaux.fr

²Dipartimento di Sistemi e Informatica, via Lombroso, 6/17, 50134 Firenze, Italy {elisa, pinzani}@dsi.unifi.it

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Abstract. Vexillary permutations are very important for Schubert Polynomials. In this paper, we consider the enumeration of vexillary involutions, that is, 2143-avoiding involutions. Instead of solving the generating function obtained by a succession system characterizing vexillary involutions, we establish a one-to-one correspondence with 1-2 trees enumerated by Motzkin numbers.

Keywords: bijection, generating tree, permutations with forbidden patterns, vexillary involutions, 1-2 trees, Motzkin numbers